Closing the Data Gap between Simulation and Modal Test with Virtualized Testing for an Improved FE Model Update

Joerg Sauer\textsuperscript{a}, Dhanushkodi Mariappan\textsuperscript{b}, Matthias Schuessler\textsuperscript{a}, Arend von der Lieth\textsuperscript{c}, Michael Stone\textsuperscript{c}

\textsuperscript{a} Polytec GmbH, Polytec – Platz 1-7, 76337 Waldbronn, Germany
\textsuperscript{b} TechPassion Technologies Pvt. Limited, 15-16 (Old No.2/7B) Yogi Gardens; Pallipattu, Chennai 600113, India
\textsuperscript{c} Polytec Inc., 1046 Baker Road, Dexter, MI 48130, United States

1 ABSTRACT

FE model validation requires building prototypes and performing experimental modal analysis. The established procedure for FE model validation requires leaving the CAE world, stepping into manual procedures for acquiring the data for experimental modal analysis and feeding the results back into the CAE data chain.

A new approach is described, which allows to keep the CAE data chain also for the physical test. This approach makes use of the properties of an optical laser vibration probing system combined with robotics. Optical methods allow working with measurement grids which are derived from existing FE models of an object under test (OUT). Being free from the constraints of physically mounted and cabled sensors, two major shortfalls of conventional testing methods are overcome: the limited spatial density of measurement nodes and mass loading. Overcoming those constraints, the MAC values between measurement and simulation are considerably improved which allows for a much better quality of the FE validation.

The new method uses the object coordinate system from the FE model. An easy to perform alignment method allows for matching the coordinate system of the OUT with the simulation. A robot program is generated representing an envelope to the OUT. The robot moves along trajectories allowing a sensor system to cover the full surface of the OUT. A 3-dimensional scanning laser Doppler vibrometer (SLDV) is used to acquire the full field frequency response of the undistorted modes without mass loading from instrumentation.

The measurement is performed with three lasers pointing to the nodes of the measurement grid each from a different direction, recording the vibration information along each of the three directions. Image processing methods guarantee the three lasers to overlap on the structure. At the same time, deviations between the coordinates from FE and the real geometry are recorded automatically. The FRFs are acquired directly at the nodal points in the coordinate system of the OUT. The results of the subsequent experimental modal analysis can be transferred to the CAE program without interpolation.

The contactless modal testing method makes use of and integrates into an existing CAE data pool of the automotive industry. The method has proven to deliver datasets suitable for a more precise FE model update in considerably shorter time compared to current procedures.
2 INTRODUCTION

In order to reduce costs and improve time-to-market, NVH studies today rely heavily on the simulation process. Fewer prototypes are being built, which results in the need for significantly more thorough testing than in the past. This requires improved test productivity, data reliability, density and accuracy.

Experimental modal analysis (EMA) is the test method to generate data required for the verification and the update of Finite Element models. Although well established, EMA is traditionally a labor intensive process requiring the attachment of accelerometers and cables to the object under test.

Meshes for FE calculations typically contain several thousands of nodes. Limited availability of accelerometer channels and high sensor cost limit the number of simultaneous measurement points to around 10…100. For a proper update of the FE model, a certain number of modes must be identified in the experimental data, therefore, reasonable high Modal Assurance Criterion (MAC) values between simulated and measured modes should be aimed.

In many cases, more locations should be measured than accelerometers or channels are available. For larger objects the accelerometers are therefore moved to several sets of locations and the test is repeated. To keep the overall dynamic conditions fixed, dummy masses can be used to replace sensor masses. The total masses need to be taken into account, when validating the FE model. For some structures it is impossible to completely model the effects of the added masses in the simulation.

The challenging task for the Noise, Vibration and Harshness (NVH) test lab is to acquire the necessary frequency response functions (FRF) in the correct coordinate system at the optimum locations and in the right orientation. In addition to the resulting time and cost constraints, the entire process of conventional measuring with accelerometers is subject to human errors. The influence on the test results will be discussed in paragraph 5.

This paper describes a fully integrated testing system to provide feedback for updating and refining the CAE models. The new method relies on the non-contact scanning laser Doppler vibrometry combined with robotics. The development of the system was guided by the idea to fully automate the EMA process in order to significantly increase the data quality combined with an increased throughput of the lab.

3 SCANNING LASER DOPPLER VIBROMETRY

A common approach for non-contact experimental modal analysis is scanning laser Doppler vibrometry (SLDV). Scanning laser Doppler vibrometers, introduced in the 1980s [1], are systems for non-contact measurement of vibration utilizing the optical Doppler effect, which causes a shift in the frequency of light backscattered from a moving surface.

The frequency shift is given by the formula: \[ \Delta f = \frac{2v}{\lambda} \] (eq. 1)

Where \( \lambda \) is the wavelength of the laser, typically a visible HeNe laser operating at 632.8 nanometers and \( v \) is the velocity of the surface.

Frequency decoding electronics produce a real-time output signal proportional to instantaneous velocity of the surface relative to the sensor in the direction of the laser. Galvanometer-driven mirrors scan the laser over the test surface in order to obtain vibration data at each predefined location. Because the vibrometer output is directional and can be acquired, stored and processed in the same way as signals from an accelerometer, it is possible, using FFT signal processing together with multi-channel data acquisition, to acquire all of the information required for a modal analysis. Additional channels are used to simultaneously gather data from other sources such as load cells, accelerometers, microphones.
A complete experimental modal analysis for model updating requires the vibration amplitude and phase spectra in all three orthogonal axes of the test object's coordinate system. It also needs to know the geometric shape of the object under test and the exact coordinate location of each measurement. This information is provided by a three dimensional SLDV which will be explained in paragraph 6.1.

4 CAE DATA CHAIN

The generation of FE models from the initial design of a component is the starting point for the NVH optimization. Depending on the complexity regarding shape and material parameters a mesh is generated which ideally represents the later prototype. The FE model should allow predicting the dynamic and durability parameters of these components for a defined operating condition. In the discussed case the results of the modal analysis, Eigen modes and Eigen frequencies need validation in an experimental modal analysis on the physical prototype.

The resulting data, deflection shapes, frequency response functions and – after modal extraction – experimental mode shapes and damping values are used to update the FE model.

FE models contain at least several thousands of nodes. In practice a measurement for validating the FE model contains only a subset of the FE nodes. In other words: the measurement is incomplete. This incompleteness is described by the term incompleteness ratio:

\[ i_r = \frac{n}{N} \]  

(eq. 2)

Where \( n \) is the number of measured nodes and \( N \) the number of nodes in the FE model.

Other authors have shown that the quality of an FE model update strongly depends on the incompleteness ratio. E.g. Grafe states: “It is a characteristic feature of large applications that the FE models are usually large and, more importantly, the number of available measurements is comparatively small. … The real challenge of updating large FE models is not so much the size of the models, as these can be solved by ever more powerful computers, but rather small incompleteness ratios” [2]. In other words: the number of measurement nodes must be sufficiently high to ensure a correct update of the FE model.

5 DISCUSSION OF THE CONVENTIONAL APPROACH FOR MODAL TESTING

In order to validate the results for a modal test derived from an FE simulation, a sample is probed by accelerometers attached to the surface. With the measured input force, frequency response functions (FRFs) are recorded at a predefined number of measurement points.

While the CAE process works with closed data links between CAD and FEM these links are lost when entering the physical test phase in the conventional way. The main reason is the manual instrumentation of the test sample. The approach to close this gap consequently must include an automated system for the acquisition of data which works with test descriptions based on the data from CAE.

This well established method introduces some sources of error into the test process. The quality achieved will result in a reduced accuracy of the later FE model update and may cause additional iterations. The sources of error are
The number of available sensors is limited. Thus one has to decide for the highest mode for the later MAC analysis and the model update based on the test effort.

- The correlation of the sensor position and the FE object coordinate system is basically lost. I.e. the position and especially the orientation of the tri-axial sensors with their inherent x, y, z coordinate systems have to be determined manually in order to match the object coordinate system.
- Depending on the mass on the OUT the sensor mass including fixtures and cables is changing the resonance frequencies of the structure. This effect can be compensated in the FE model by adding the respective mass at the nodal points selected for the sensors. If the OUT cannot be measured in one set, because the number of available acquisition channels is not sufficient, dummy masses can be used to compensate for the sensor mass while the sensor is not mounted.

The sources of error become more significant the more lightweight and the more complex-shaped a structure is.

6 NEW MODAL TESTING APPROACH INTEGRATED IN THE CAE PROCESS

6.1 3-D LASER DOPPLER VIBROMETRY

As already stated, a laser Doppler vibrometer measures the vibration component in the direction of the laser beam. With three laser vibrometers it is possible to determine the three-dimensional motion of a surface by focusing three laser beams from three different, known directions onto the measurement point. Through a coordinate transformation matrix, the measured data is transformed into a right-angled coordinate system. For this to work it is not necessary to align the lasers at right angles to each other.

The following equation represents the unit vector which expresses the laser beam direction of the first scan head:

\[ L_1 = \begin{pmatrix} l_{1x} & l_{1y} & l_{1z} \end{pmatrix} \]  

(eq. 3)

The matrix below contains the directional information of all three laser beams. It is used to transform the three measured vibrometer signals \( (v_1, v_2, v_3) \) into the orthogonal object coordinate system \( (v_x, v_y, v_z) \):

\[
\begin{pmatrix}
  v_x \\
  v_y \\
  v_z \\
\end{pmatrix}
= \begin{pmatrix}
  l_{1x} & l_{1y} & l_{1z} \\
  l_{2x} & l_{2y} & l_{2z} \\
  l_{3x} & l_{3y} & l_{3z} \\
\end{pmatrix}^{-1}
\begin{pmatrix}
  v_1 \\
  v_2 \\
  v_3 \\
\end{pmatrix}
\]

(eq. 4)

If the lasers are to be scanned over the surface, all three lasers must strike the same location for each scan point. In order to do this, the system must be taught the relative position of the three scan heads in the coordinate system of the OUT. This procedure, known as 3-D alignment (first described in [3]), is performed through software by orienting the three laser beams so that they merge onto a single point. If the coordinate of this point is known, the deflection angles of the scan mirrors are recorded and the procedure is repeated at 3 additional points, the orientation of the sensor heads in the coordinate system can be determined [4].

By providing the system with the exact geometry of all points to be measured during the scan (not just the points used for the 3-D alignment), the lasers will always merge to a single location for every scan point via software.

The 3D-SLDV developed by Polytec uses a time-of-flight laser distance sensor, operating through the scan mirrors, coaxial with the laser vibrometer, to experimentally determine the geometry of the structure (Geometry Scanner). Even better positioning accuracy can be achieved through "VideoTriangulation" of the three laser
beams on the sample. This is performed using image processing to determine the point of impact of the 3 laser beams. The position information is then used to merge the points and thus determine the true surface position.

Alternatively, geometry files in Universal File Format (UFF) can be imported into the system. This geometry information can be displayed as a 3-D plot and the vibration data superimposed over it. A file comprising the measured geometry can also be exported into the simulation program together with the 3-D vibration data. The ability to measure geometry as well as vibration can be very useful when for example benchmarking a competitor’s product.

If the geometry of the FE model does not exactly match to the geometry of the physical prototype, the 3 laser points do not merge at the surface. In this case VideoTriangulation can be used to merge the points and thus determine the true geometry. The corrected geometry model can then be transferred back into the CAE system to update the FE model.

If there is no numerical model available, e.g. for benchmarking tests, the 3D-SLDV can measure the geometry by the integrated time-of-flight laser distance sensor.

The data can be presented as a color-coded 3-D animation of the Operating Deflection Shape (ODS) at any selected frequency of interest. 3-D vibration components can either be visualized simultaneously or separately in any combination of v_x, v_y and v_z. The software together with an 8-channel data acquisition system is capable of performing Multiple Input Multiple Output (MIMO) modal testing.

### 6.2 COMBINING 3-D SCANNING LASER VIBROMETRY WITH ROBOTICS

In order to measure the complete surface of a complex three-dimensional object such as the car body in Figure 5, the three scan heads need to be moved to a number of locations and the relative position of the scan heads to the object need to be re-taught for each location. The data from each scan head array position can be stitched together into a single file using reference points with known coordinates on the test surface.

Since it could take as many as twenty different positions of the scan head array to measure the entire surface of an automobile body, an automated approach that avoids twenty 3-D alignment steps saves a considerable amount of time and effort.

An industrial robot is designed to have all of the flexibility of a human arm and hand, and can have the load capacity and stability needed to accurately position three SLDV scan heads plus fixtures and cabling. Furthermore it is controlled via computer so that the relative x, y and z position of the object it is holding can be controlled and continuously monitored. The robot used in this paper has three rotation axes in its arm and additional three rotational axes in the hand. A seventh linear axis is used to extend the reach of the robot arm. Potentially, whole aircraft fuselages could be measured using this approach.
The scan heads are fixed relative to the robot flange. The 3-D alignment procedure described above only needs to be performed one time during installation in order to obtain the scan head positions and orientations relative to the robot flange. The robot control software can automatically calculate from the robot’s coordinates the positions and orientations of the scan heads relative to the test object at any time.

During installation, the 3-D alignment is performed on coordinates in the so called TOOL coordinate system. The TOOL coordinate system is defined relative to the robot’s flange and moves together with the robot. The TOOL position and orientation can be retrieved from the robot controller.

A second robot coordinate system called the BASE system is calibrated to coincide with the test object’s coordinate system. This calibration uses all three lasers which, by moving the robot, are made to intersect at each of several calibration points on the test object with known coordinates. The BASE coordinate system is calculated from the robot positions and the corresponding object coordinates.

With 3-D alignment having been performed in the TOOL coordinate system and the BASE coordinate system calibrated on the test object, the scan head positions in the test object’s coordinate system can be automatically calculated for any robot position.

The geometry information can either be imported or measured using the integrated geometry laser.

Before the measurement is started, the robot positions and their sequence are defined by teaching. Based on those taught positions, the control software decides which point is to be measured from which position.

Figure 5: Simulation of twin-RoboVib test cell, each robot on a linear track
7 CASE STUDY: MODAL UPDATING ON A GEARBOX COVER

To compare the new automated approach with the conventional manual accelerometer measurement, two sets of measurement with subsequent modal analysis are performed. As a sample, a cast alloy side-cover of a motorcycle gearbox was used.

![Gearbox cover](image)

<table>
<thead>
<tr>
<th>Model Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Mesh Type</td>
<td>Tetrahedral</td>
</tr>
<tr>
<td>Elements</td>
<td>69019</td>
</tr>
<tr>
<td>Nodes</td>
<td>19994</td>
</tr>
<tr>
<td>Material</td>
<td>Aluminum cast alloy</td>
</tr>
</tbody>
</table>

Figure 6: Gearbox cover for case study and parameters of the FE model

The modal analysis performed upon the FE model was used to compare the results of the two testing approaches in the subsequent MAC analysis.

7.1.1 Conventional Test with Accelerometers

![Cover with marked locations](image)

- Boundary condition: free-free
- Excitation: modal hammer with force cell
- Measurement locations: 14 measurements points / 42 DOF
The gear box cover was probed with conventional triax accelerometers under free-free conditions. Figure 8 illustrates the corresponding FE-updating process. The locations for measurement are chosen manually, the instrumentation is also a manual process. The results (see figure 13) show the 1\textsuperscript{st} and 2\textsuperscript{nd} mode, both below 1 kHz.

Figure 8: FE model updating process in VMAP with accelerometers
7.1.2 Automated Test with RoboVib®

- Boundary condition: free-free
- Excitation: automated modal hammer with force cell
- Measurement locations: 1630 scan positions / 4890 DOF

Figure 9: Test Setup with PSV-3D and RoboVib

The measurement procedure is completely automated. Communications between the robot control and measurement software are performed over a network via OPC client/server architecture. The robot sends a signal when it has moved to a new location and is ready for the lasers to begin scanning again. There is also a signal from the measurement system to the robot when the laser scan has finished and the system is ready for the robot to move to the next position.

The diagram in Figure 10 shows the complete CAE-integrated measurement workflow from test structure preparation and set-up through FE model updating.

Figure 10: Robot-based SLDV workflow diagram

In order to optically scan the complete cover the robot was taught with positions from all sides of the cover. After preparing the measurement on daytime, the measurement was running over night. Data from 1630 nodes was acquired automatically. Results from all robot positions are automatically stitched together into a single seamless file for analysis. The post-processing is performed in the VMAP Modal Analysis package.
Imported FE mesh. 10076 nodes

Figure 11: Imported and coarsened FE mesh

coarsened measurement grid: 1630 nodes

Figure 12: FE model updating process in VMAP with PSV-3D and RoboVib®
The results of the first two modes for the different measurement techniques are displayed in figure 13. As reference those first two modes from FEA are also depicted in figure 13.

![Comparison of mode shapes of FEA with RoboVib® and conventional measurements](image)

**Figure 13: Comparison of mode shapes of FEA with RoboVib® and conventional measurements**

### 8 MAC ANALYSIS

One major application of the system is to be able to compare and update finite element models (FEM). For this purpose the complete spectral data files for all measurement points can be exported to an experimental modal analysis program via Universal File Format data transfer where modal parameters (natural mode shapes, Eigen frequencies and modal damping) can be calculated from the measured transfer functions. In this case the modal analysis program VMAP from TechPassion was used. It offers a native import of Polytec's binary file format, without the prior conversion into Universal File Format. Similar examples can be found in [5, 6]. The mode shapes and Eigen frequencies can be compared to the values calculated from the simulation and the modal damping can be added to the FEM. The FEM can now be tuned to the real structure and an improved model can be derived using VMAP FE model updating tools.

#### 8.1 Accelerometer test

The modal analysis from the conventional accelerometer test was limited to the first 2 modes at 592 Hz and 933 Hz. The MAC values between the same modes from measurement and simulation are 0.67 and 0.59. These values lead to the conclusion, that some parameters of the test, e. g. accelerometer masses and the location and orientation of the sensors have a lowering influence on the quality of the measurement.
Figure 14: Modal Assurance Criterion (MAC) in VMAP comparing FEA and triaxial accelerometer measurements

8.2 RoboVib® Test

Using a 100 times higher point resolution allows to extract also higher modes of the gear box cover. The MAC values between the same modes from measurement and simulation are close to 1, showing a much better match compared to the accelerometer test. Figure 15 shows the MAC matrix for the first five modes, the diagonal values are close to 1 and the off-diagonal values are close to zero which allows for a clear assignment of the measured modes to the simulated modes.

Figure 15: Modal Assurance Criterion (MAC) in VMAP comparing FEA and RoboVib measurements
9 SUMMARY AND CONCLUSIONS

As stated before, measurements with the robot-based system presented here ensure that the measurement grids correspond precisely with the FEM grids and conveniently allow automatically-generated FEM coordinates to prepare the measurement points. This method eliminates a degree of complication and improves productivity. The model updating can be more precise, faster and more efficient.

It can be expected that even with the same locations and no influence of the sensor mass the values from the RoboVib test will deliver higher MAC values, due to the reduction of other sources of error like the orientation and geometrical match of the results to the nodal points.

Incompleteness ratio is the ratio of the number of measurement data points and FEA nodes. The finite element model updating algorithms perform best with high incompleteness ratio. In other words, it is important to use as many measurement points as possible. But, this is a time-consuming process. The new RoboVib® scanning laser Doppler vibration measurement system explained in this paper allows for one or two orders of magnitude higher point numbers, and therefore, gives the maximum productivity and accuracy in the FEA-Test correlation and model updating activity.

REFERENCES